

Ab initio Calculations on Octahedral $(\text{CH})_x(\text{NH})_{6-x}$

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Octahedral 38-, 44- and 48-electron systems are closed-shells and could be stable. The latter two systems have a high energy and dissociate via a non-symmetric path. $(\text{NH})_6$ in a chair conformation should be stable.

Key words: Octahedral $(\text{CH})_x(\text{NH})_{6-x}$ – Chair N_6H_6

In recent investigations Hogeveen and Kwant found $(\text{CH})_6^{++}$ to possess C_{5v} -symmetry [1]. One could go one step further and consider $(\text{CH})_6^x$ in octahedral symmetry. In this contribution we study this possibility with *ab initio* calculations. In order to be stable, first-order Jahn-Teller instabilities should not exist, i.e. no partially filled degenerate orbitals are permitted. Consider six NH-fragments, possessing 48 electrons, in octahedral conformation (point group O_h). The 1s-orbitals split up to yield one a_{1g} -, one e_g -, and one t_{1u} -orbital. A similar situation holds for the N–H bonds, and the nitrogen lone pairs add the third a_{1g} , e_g , and t_{1u} . The N–H “ π ”-orbitals combine to form the fourth t_{1u} , and one t_{2g} . However, a calculation of $(\text{NH})_6$ shows an occupation 1– $3a_{1g}$, 1– $3e_g$, 1– $3t_{1u}$, 1 t_{2g} , 1 t_{2u} . The t_{1u} - and e_g -combination of the lone pairs are lying fairly high due to the crowding of these orbitals in the hole of the octahedron. The 4 t_{1u} -orbital is so high in energy that a t_{2u} -orbital will be occupied preferentially. One of the components of the t_{2u} -orbital, triply degenerate, is shown in Fig. 1. It is seen to be antibonding, but interestingly, dissociation of a system in which this orbital is occupied into the corresponding 2+2+2, 3+3, or 4+2 first-row atom monohydrides is symmetry-forbidden. The 44-electron system, in which the high-lying $3e_g$ -orbital is now unoccupied, thus exhibits the same features. A calculation on a 38-electron system finally shows the t_{2u} -orbital to be unoccupied. These compounds, closo- $(\text{CH})_2(\text{BH})_4$ are known to be stable [2, 3]. We performed the

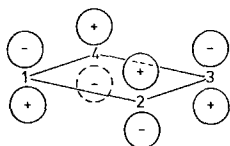


Fig. 1. One of the components of the t_{2u} -orbital

calculations with a minimal STO-3G basis set; in some cases a minimal STO basis set was used. The geometry of all compounds discussed was optimized. We calculated the energies of several 48- and 44-electron systems suggested in the MO-analysis. For the former $(\text{NH})_6$ is suited, for the latter apart from $(\text{CH})_6^-$ a partial carbon and nitrogen composition may be acceptable.

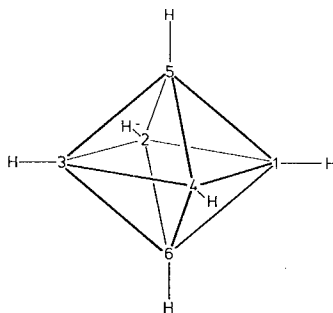


Fig. 2. Octahedral $(\text{XH})_6$

Octahedral $(\text{NH})_6$, having N–N bond lengths of 1.84 Å is calculated 702 kcal/Mole endothermic compared to three molecules *cis*- $(\text{NH})_2$. The highest occupied orbitals, $3e_g$ and $1t_{2u}$, have Ionization Potentials (IP's) of about 4 eV. These orbitals reflect the inability of nitrogen to behave like a pentavalent atom, and must be held responsible for the instability of the system.

Table 1. Compounds discussed and calculated energies at the optimal geometry

Compound	Calculated Energy (a.u.) ^a	
octahedral $(\text{NH})_6$	STO	– 327.7682
chair $(\text{NH})_6$ H axial	STO	– 329.0297
octahedral $(\text{CH})_6^-$	STO	– 228.6519
<i>cis</i> -HNNH	STO	– 109.6289
chair $(\text{NH})_6$ H axial		– 325.7795
chair $(\text{NH})_6$ H equat.		– 325.7348
octahedral $(\text{CH})_2(\text{NH})_4^{+}$ (1,3-C)		– 291.6050
octahedral $(\text{CH})_3(\text{NH})_3^{+}$ (1,2,5-C)		– 275.7728
octahedral $(\text{CH})_4(\text{NH})_2$ (1,3-N)		– 259.3944
<i>cis</i> -HNNH		– 108.5453
<i>trans</i> -HNNH		– 108.5570
<i>cis</i> -HCNH (RHF)		– 92.1752
HCNH ⁺		– 91.9978
HCCH		– 75.8562
triplet NH (RHF)		– 54.2593

^a 1 a.u. = 27.21 eV = 627.2 kcal/Mole.

Addition of 2s- and 2p-polarization functions at the center of mass, representing the influence of a caught small cation, brings the energy firmly down, but can do

little for the $3e_g$ - and $1t_{2u}$ -orbitals, which in a united-atom approach form d - and f -functions.

$(\text{NH})_6$ is isoelectronic with $(\text{CH}_2)_6$, cyclohexane. In a chair form with all nitrogen atoms tetrahedral the STO-3G calculations predict the more stable conformer with axial hydrogen atoms and all $r(\text{N}-\text{N})=1.47 \text{ \AA}$ to be 68 kcal/Mole resp. 90 kcal/Mole exothermic with respect to three molecules *trans*- $(\text{NH})_2$ resp. *cis*- $(\text{NH})_2$; the results of the STO-calculations are in complete accordance with this prediction. The corresponding $2+2+2$ dissociation is symmetry-forbidden analogous to the symmetry-forbidden dissociation of benzene into three molecules acetylene. Consequently, $(\text{NH})_6$, although experimentally unknown, might be stable.

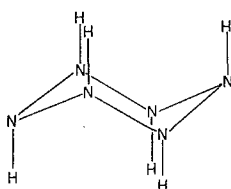


Fig. 3. The stable $(\text{NH})_6$

Generally speaking the stability of the 44-electron systems will be increased with respect to the 48-electron systems as the antibonding $3e_g$ -orbital is unoccupied.

The octahedral di-anion of benzene, $(\text{CH})_6^{--}$, may be thought of as built from two cyclopropenyl anions. It is questionable whether this species is stable itself; on combination of two such ions a large (dominant) price in Coulomb-energy has to be paid. Moreover the $1t_{2u}$ -orbital lies at nearly $+12 \text{ eV}$. This system cannot possibly exist.

Possibly stable 44-electron systems are $(\text{CH})_4(\text{NH})_2$ and $(\text{CH})_3(\text{NH})_3^+$. There is retention of approximate octahedral symmetry for *trans*- $(\text{CH})_4(\text{NH})_2$ (in Fig. 2: 1, 2, 3, 4=C, 5, 6=N), as follows from the distances from the origin (center of mass): $r(\text{O}-\text{N})=1.230 \text{ \AA}$, $r(\text{O}-\text{C})=1.147 \text{ \AA}$. Also this retention is clear from the output vectors. Therefore we will keep referring to these structures as octahedral. Some polarization is present: according to a Mulliken population analysis the NH-groups bear 8.0 electrons, the CH-groups bear 7.0 electrons. In point group D_{4h} the occupied t_{2u} -orbital splits into an e_u - and a b_{2u} -orbital, having IP's of 2.8 and -0.9 eV . Even though this last result is surely due to truncation of basis set – a larger basis set will bring this orbital down into the binding region [4] – it forms an indication for the instability of this molecule. This molecule is 509 kcal/Mole endothermic with respect to the $2+2+2$ dissociation. $(\text{CH})_4(\text{NH})_2$ (1, 2=N) is higher in energy and less attractive. On optimizing the geometry of $(\text{CH})_3(\text{NH})_3^+$ (1, 3, 5=C) this compound is found to dissociate into two fragments and $(\text{CH})_3(\text{NH})^+$. This is a consequence of the fact that the t_{2u} - and the t_{1u} -orbital are no longer distinguishable in this C_{2v} -subgroup: both are converted into an a_1 -, b_1 - and b_2 -orbital.

$(\text{CH})_3(\text{NH})_3^+$ (1, 2, 5=C) is 393 kcal/Mole endothermic with respect to its 2+2+2 dissociation products. The IP's of the $1t_{2u}$ -orbital, in C_{3v} , the e_u - and a_{2u} -orbitals, are about 12.1 eV. The distortion of octahedral symmetry is somewhat larger for this compound.

Finally non-symmetric distortions were investigated. Several possibilities in which one fragment was shifted into the direction of one or two others were calculated, meanwhile keeping all $r(\text{O}-\text{C})$ and $r(\text{O}-\text{N})$ constant. For these calculations we chose $(\text{CH})_4(\text{NH})_2$. The octahedral geometry proves to be a saddle point; a very strong preference was found for a distortion for which the symmetry of the system reduces to C_1 . We conclude therefore that despite the occupation of the $1t_{2u}$ -orbital, which precludes symmetric dissociations, these octahedral compounds cannot possibly be stable.

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References

1. Hogeveen, H., Kwant, P.: J. Am. Chem. Soc. **96**, 2208 (1974)
2. Epstein, I.R., Marynick, D.S., Lipscomb, W.N.: J. Am. Chem. Soc. **95**, 1760 (1973)
3. McNeill, E.A., Gallaher, K.L., Scholer, F.R., Bauer, S.H.: Inorg. Chem. **12**, 2105 (1973)
4. Schaefer III, H.F.: The electronic structure of atoms and molecules, pp. 252 ff. Addison-Wesley Publ. Comp. 1972

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